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Nuclear Chirality



Basic symmetries in nuclear structure

Rotational and space inversion invariance:

- result from the isotropy of space,*
- as a consequence spin and parity are good quantum numbers for nuclear states.*

Time reversal invariance:

- result from the reversibility of motion in time.*

Notation:

$R(\omega)$ –rotation,

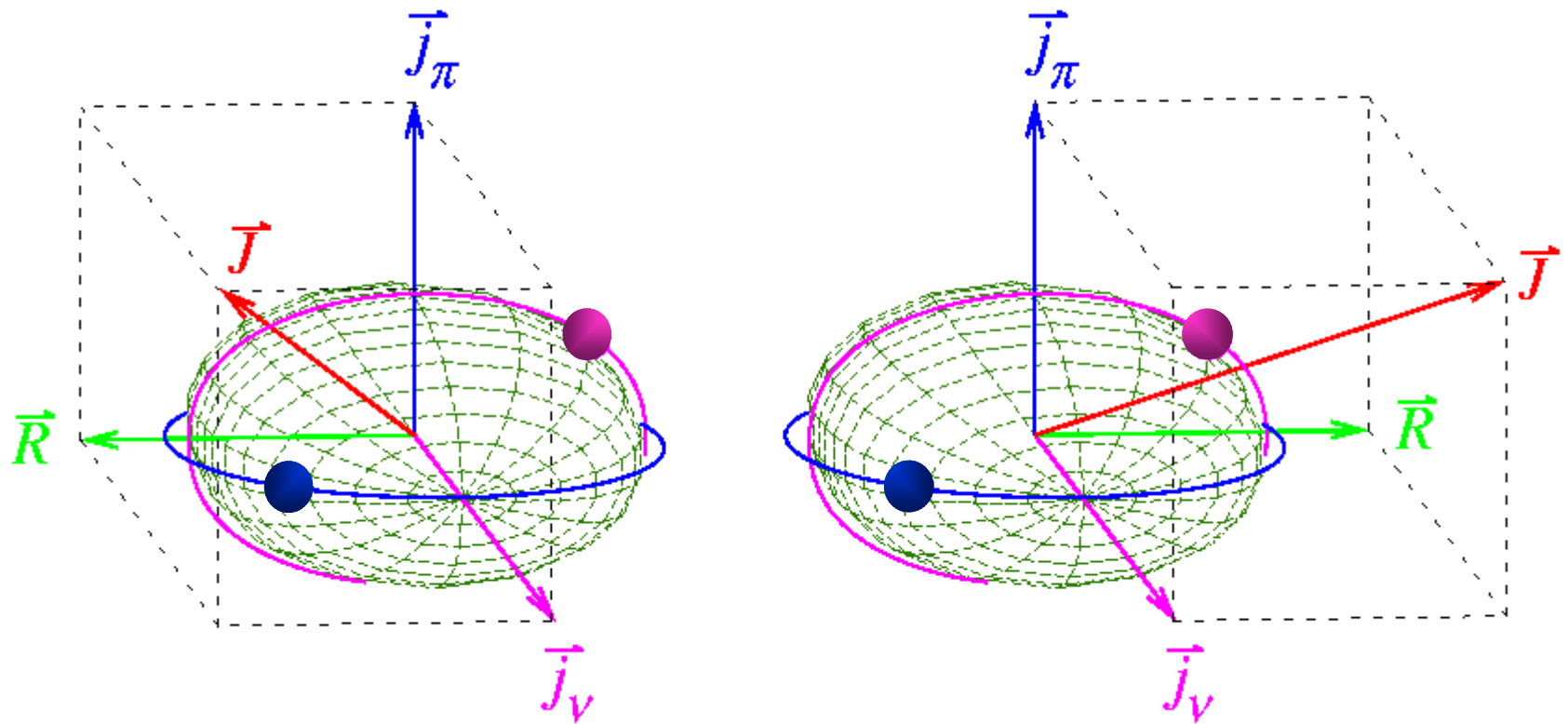
P –space inversion,

T –time reversal.

Spontaneous symmetry breaking or nuclear Jahn–Teller effect

The violation of any symmetry in the intrinsic reference frame has a profound influence on the structure of the wavefunction in the laboratory reference frame and therefore is manifest as a distinct feature in excitation modes.

Single-particle configurations in triaxial nuclei may result in three perpendicular angular momenta.



Space inversion vs time reversal:

Space inversion operation represented by \mathbf{P} is linear:

$$\mathbf{P} (a|\psi_1\rangle + b|\psi_2\rangle) = a\mathbf{P}|\psi_1\rangle + b\mathbf{P}|\psi_2\rangle.$$

For the unitary operator \mathbf{P} :

$$\mathbf{P}^2 = \mathbf{1}, \quad \mathbf{P}^{-1} = \mathbf{P} = \mathbf{P}^\dagger.$$

Eigenstates of \mathbf{P} with eigenvalues $\pi = \pm 1$ can be formed:

$$\mathbf{P} \frac{1}{\sqrt{2}} (|\text{prolate}\rangle + |\text{oblate}\rangle) = \frac{1}{\sqrt{2}} (|\text{prolate}\rangle + |\text{oblate}\rangle),$$

$$\mathbf{P} \frac{1}{\sqrt{2}} (|\text{prolate}\rangle - |\text{oblate}\rangle) = -\frac{1}{\sqrt{2}} (|\text{prolate}\rangle - |\text{oblate}\rangle).$$

If $[\mathbf{P}, \mathbf{H}] = 0$, parity is a good quantum number for nuclear states.

Space inversion vs time reversal:

Time reversal operation represented by \mathbf{T} is antilinear:

$$\mathbf{T}(a|\psi_1\rangle + b|\psi_2\rangle) = a^* \mathbf{T}|\psi_1\rangle + b^* \mathbf{T}|\psi_2\rangle.$$

For the antiunitary operator \mathbf{T} :

$$\mathbf{T}^2 = (-1)^{2I} = (-1)^A, \quad I\text{-spin, } A\text{-number of fermions.}$$

Eigenstates of \mathbf{T} can not be defined.

For the nuclear hamiltonian which is invariant under time reversal the wave functions for physical states are required to be invariant under the operator $O = T R_y(\pi)$.

T denotes time reversal .

$R_y(\pi)$ denotes rotation by 180° around the axis perpendicular to the quantization axis.

With these definitions the O operator is a complex conjugation of expansion coefficients for wave functions in $|IM\rangle$ basis.

For the planar states of three angular momenta:

$$O |IP\rangle = T R_y(\pi) |IP\rangle = |IP\rangle .$$

$$T R_y(\pi) \left| \begin{array}{c} \text{green arrow} \nearrow \\ \text{blue arrow} \uparrow \\ \text{red arrow} \nearrow \\ \text{dotted line} \rightarrow \end{array} \right\rangle = T \left| \begin{array}{c} \text{red arrow} \nearrow \\ \text{green arrow} \searrow \\ \text{blue arrow} \downarrow \\ \text{dotted line} \rightarrow \end{array} \right\rangle = \left| \begin{array}{c} \text{green arrow} \nearrow \\ \text{blue arrow} \uparrow \\ \text{red arrow} \nearrow \\ \text{dotted line} \rightarrow \end{array} \right\rangle$$

For the right- and left-handed states of three mutually orthogonal angular momenta:

$$O |IR\rangle = T R_y(\pi) |IR\rangle = |IL\rangle ,$$

$$O |IL\rangle = T R_y(\pi) |IL\rangle = |IR\rangle .$$

$$T R_y(\pi) \left| \begin{array}{c} \uparrow \\ \nearrow \\ \rightarrow \end{array} \right\rangle = T \left| \begin{array}{c} \nearrow \\ \rightarrow \\ \downarrow \end{array} \right\rangle = \left| \begin{array}{c} \nearrow \\ \leftarrow \\ \uparrow \end{array} \right\rangle$$

For $|IR\rangle$ and $|IL\rangle$ quantum mechanical analysis for a two level system directly applies.

(See for example Feynman lectures on Physics.)

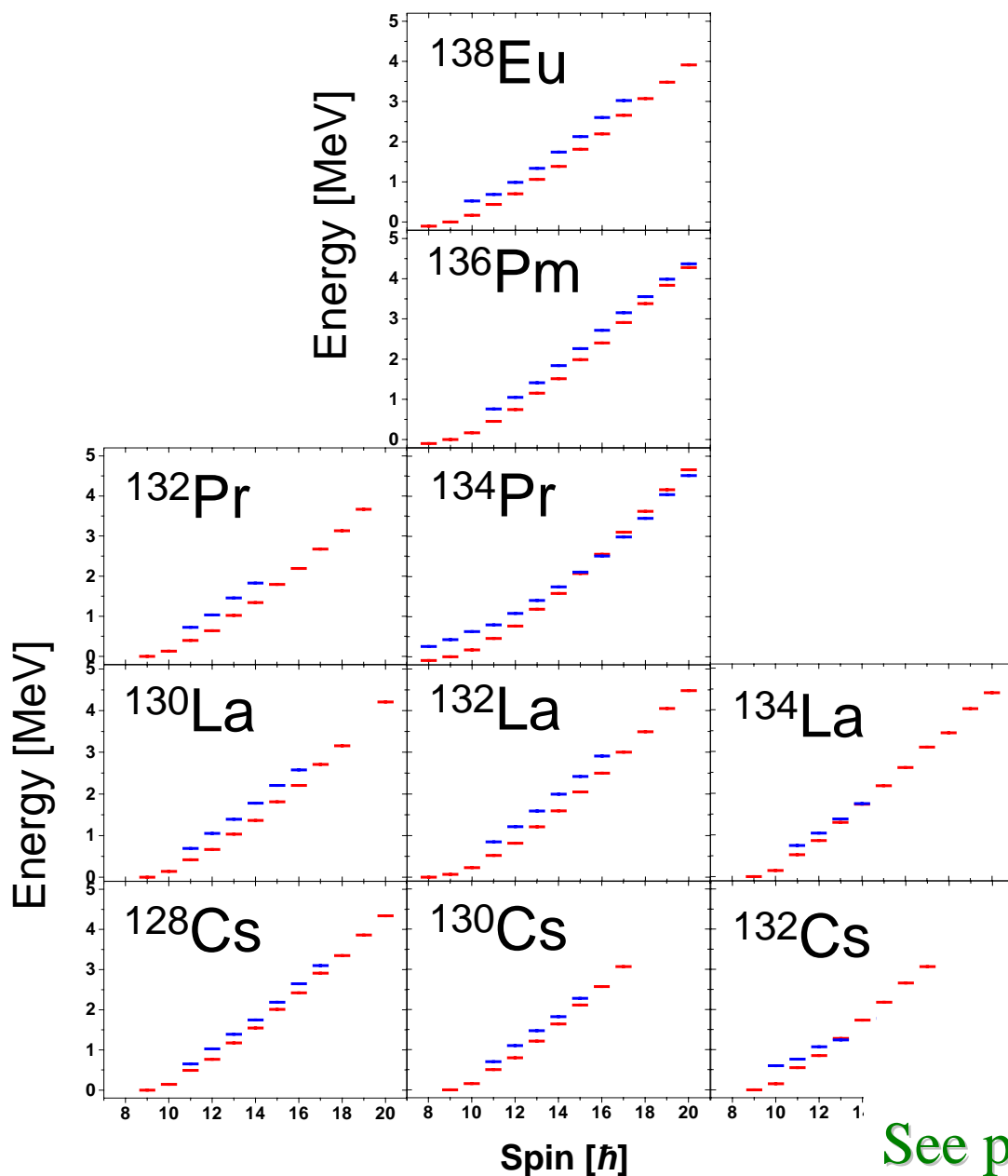
Physical states invariant under O are:

$$|I + \rangle = \frac{1}{\sqrt{2}} (|IR \rangle + |IL \rangle),$$

$$|I - \rangle = \frac{i}{\sqrt{2}} (|IR \rangle - |IL \rangle),$$

Experimental evidence for doublet bands:

Systematics of partner bands in odd-odd $A \sim 130$ nuclei.

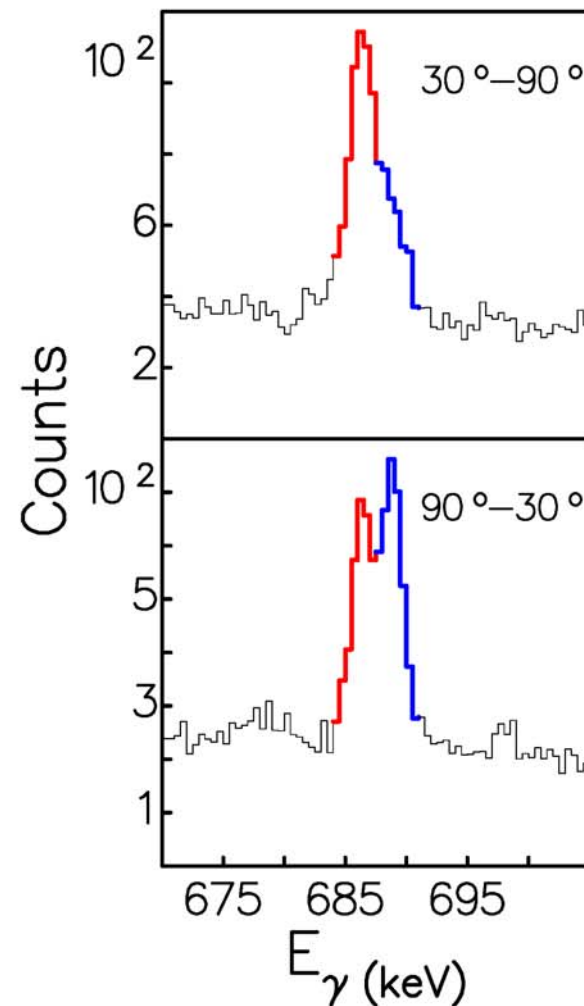
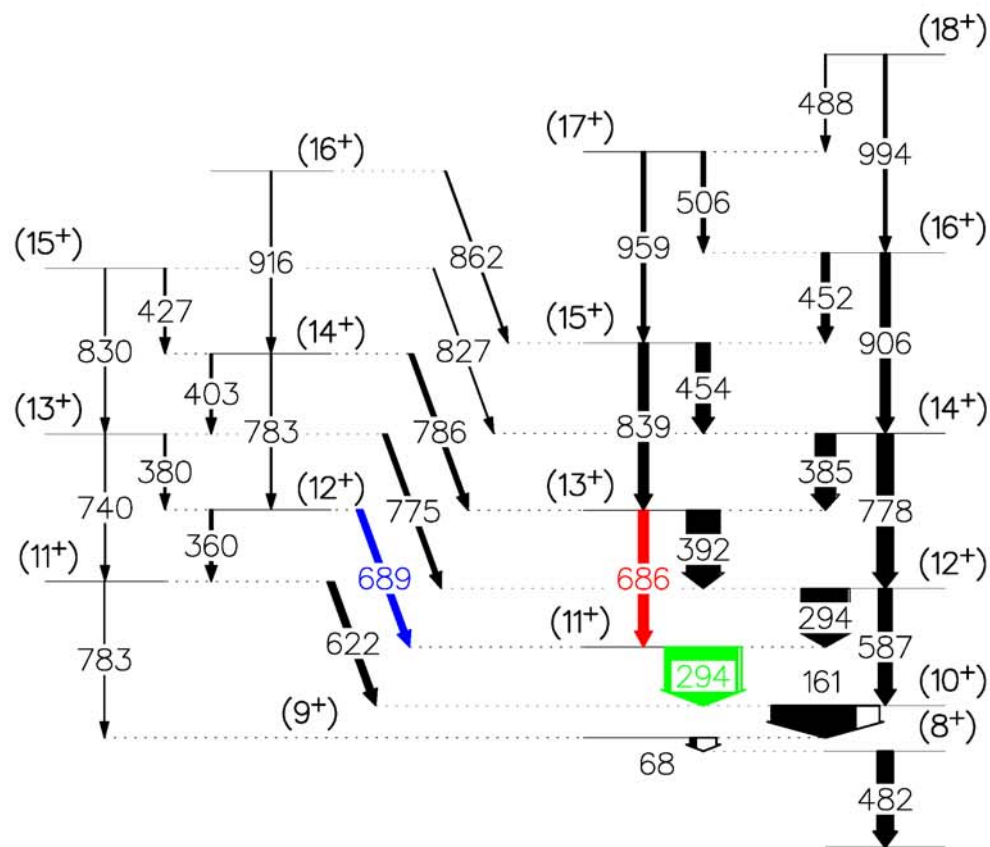


See poster of A. Hecht

Angular correlation (DCO) measurement for ^{132}La .

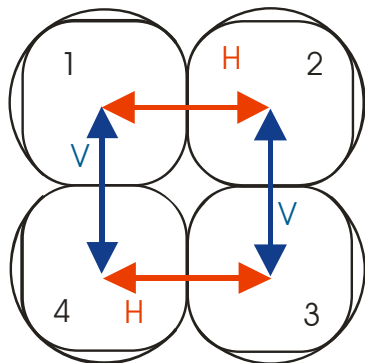
$$R_{DCO}(294 \text{ keV } M1/E2 - 686 \text{ keV } E2) = 0.46(6)$$

$$R_{DCO}(294 \text{ keV } M1/E2 - 689 \text{ keV } ?) = 1.4(2)$$



Polarization measurements in ^{132}Cs

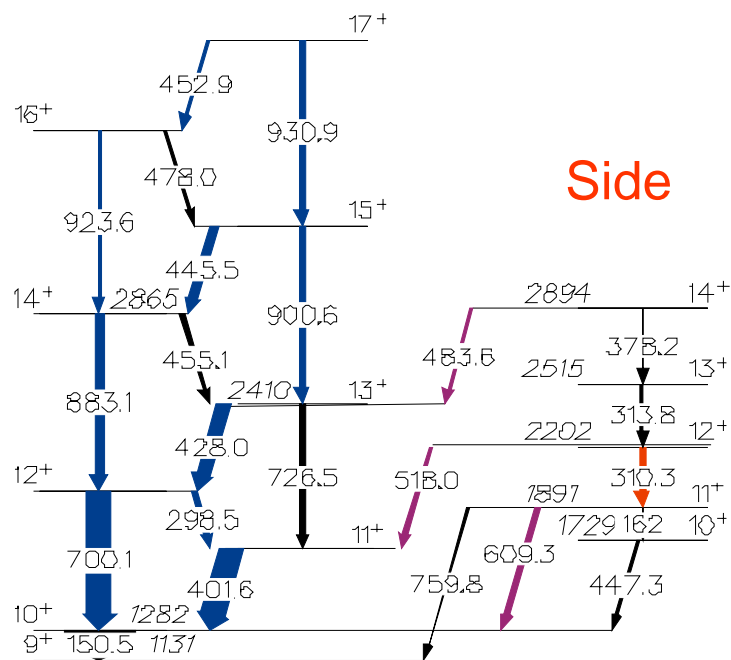
[G Rainovski et al., PRC 68, (2003) 024318].



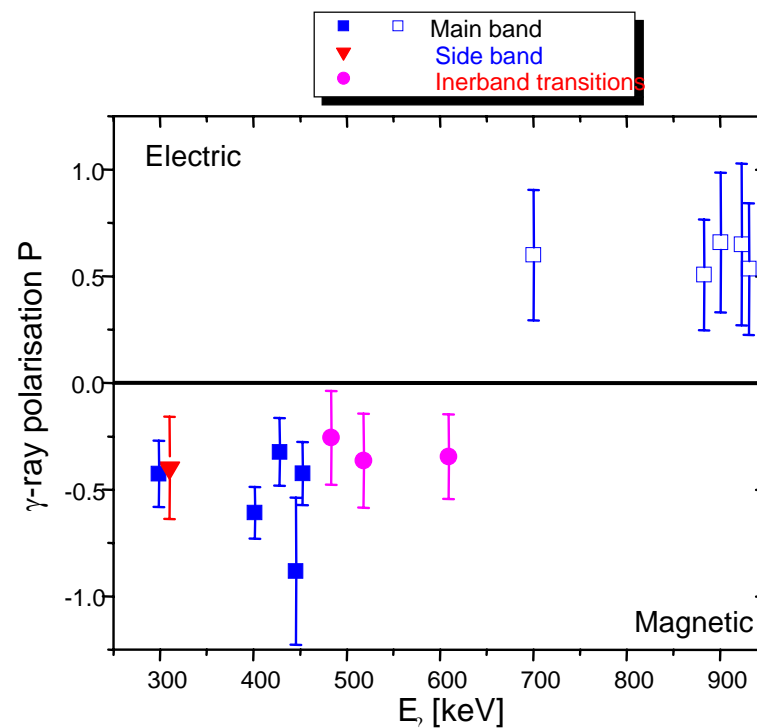
$$P = \frac{1}{Q(E_\gamma)} \frac{N_v - N_h}{N_v + N_h}$$

$Q(E_\gamma)$ – P.M. Jones et al., NIM A 362 (1995) 556

Main



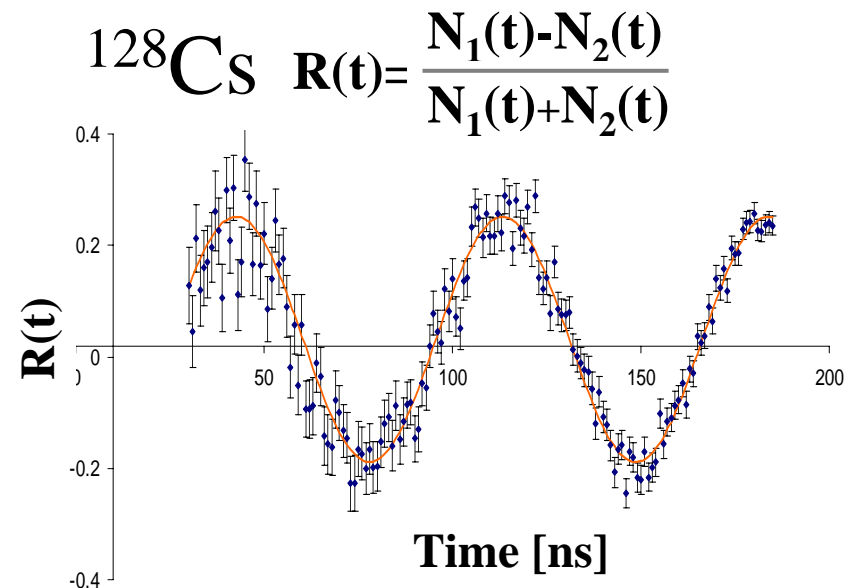
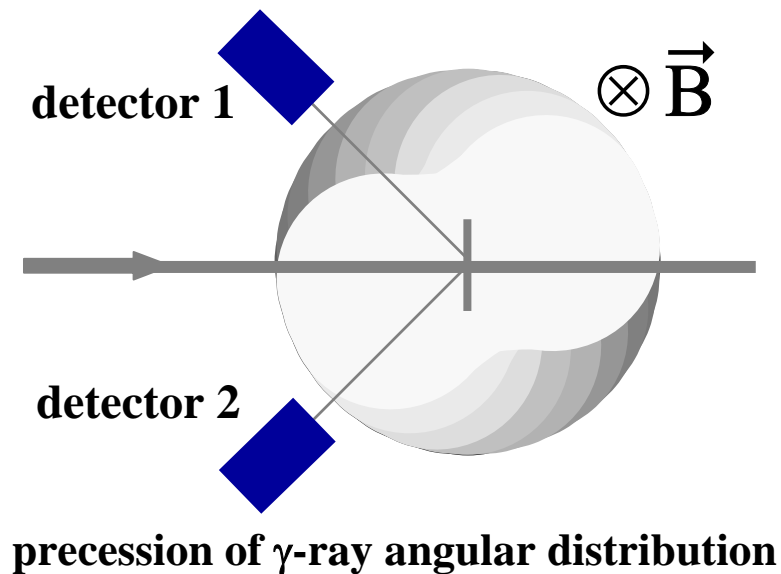
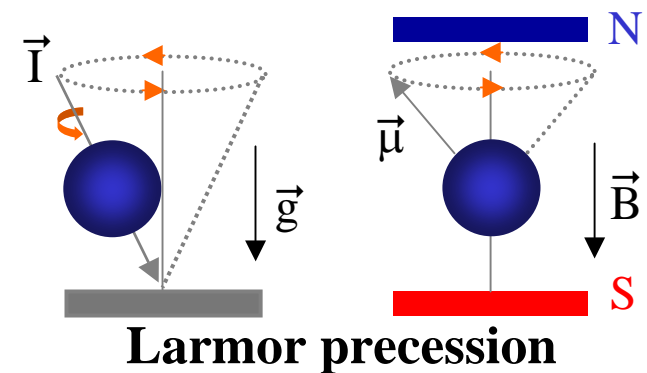
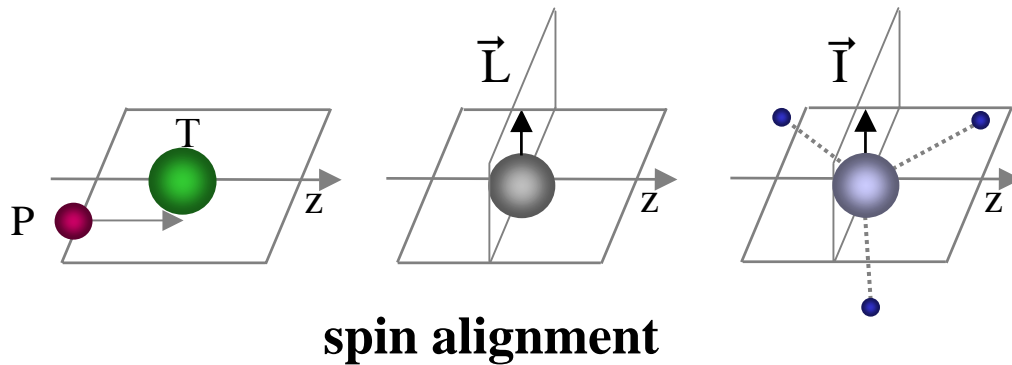
Side



The unique parity argument gives model independent configuration assignment for partner bands !

- *electromagnetic operators are one-body operators;*
- *matrix elements for M1 and E2 operators are non-zero between single particle orbitals with the same parity only;*
- *in odd-odd nuclei M1 and E2 transitions are strongly hindered between configurations involving unique- and normal-parity valence single particle orbitals, despite of the same resulting parity for observed bands;*
- *the main bands are known to be built on unique-parity orbitals;*
- *the observation of M1/E2 links yields the same configuration for the side bands as for the main bands, since no other unique parity orbitals are near the Fermi level.*

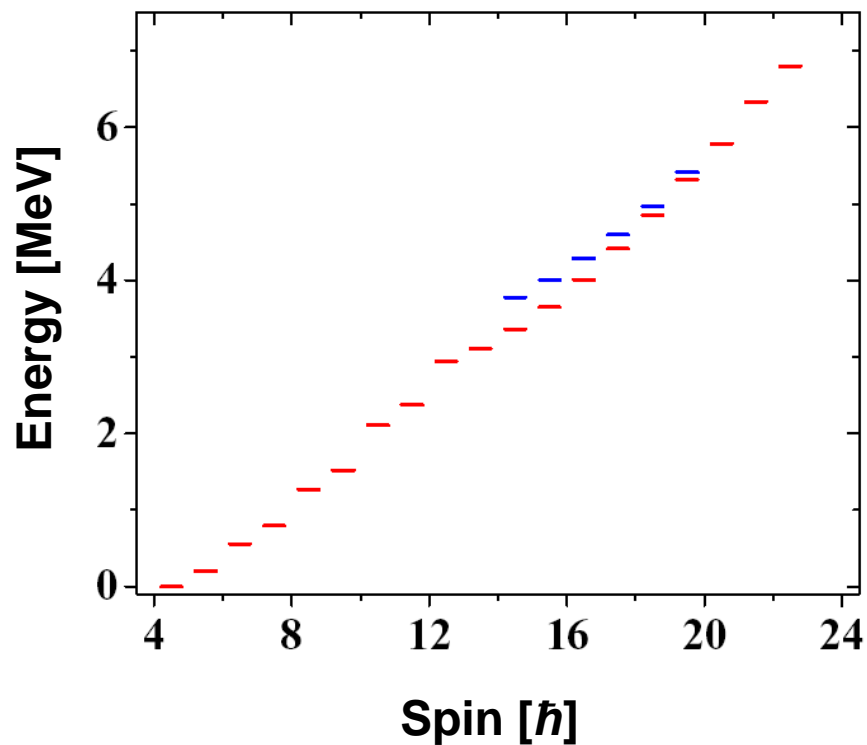
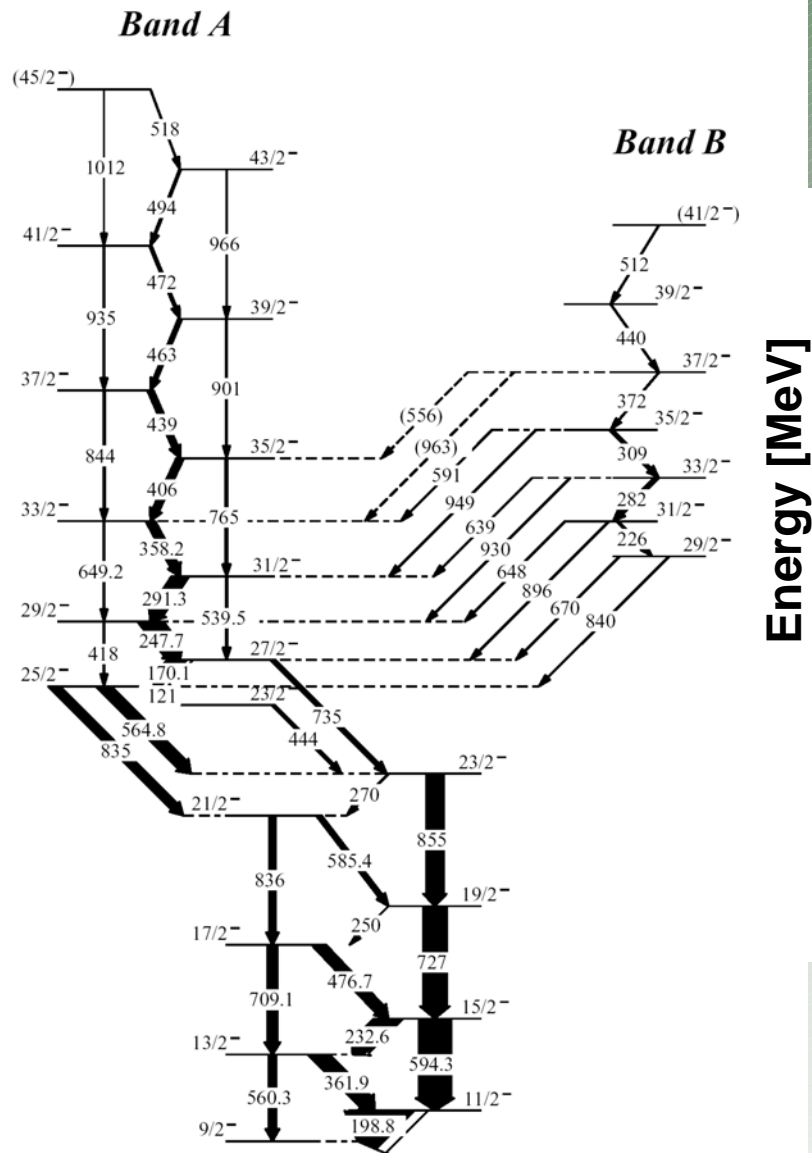
Unique parity configuration assignments for the main band from magnetic moment measurements.



T. Ahn et al. to be published.

Doublet bands in odd-even ^{135}Nd near ^{134}Pr

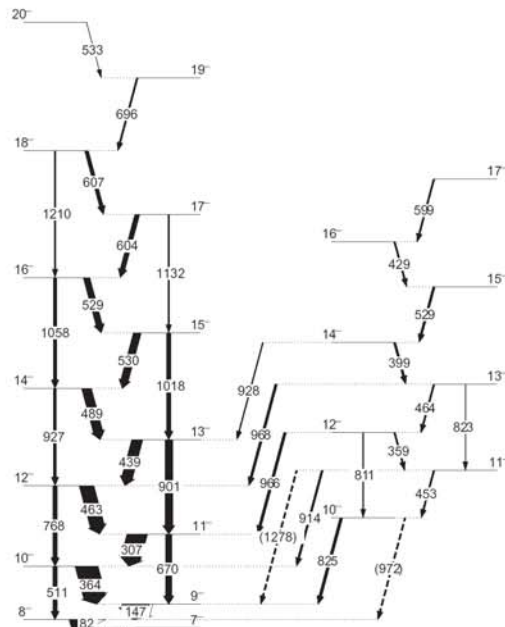
S. Zhu et al., PRL 91(2003) 132501.



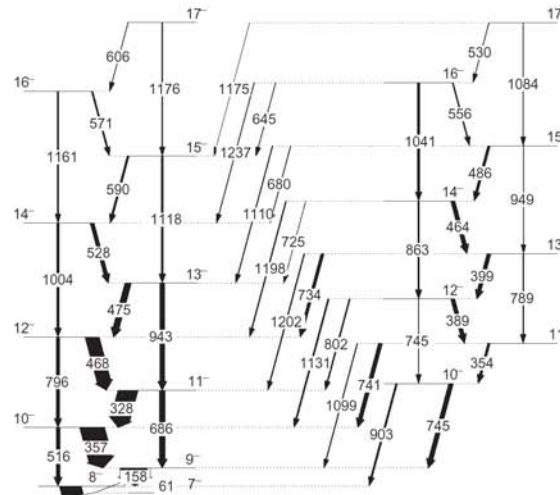
Systematics of odd-odd Rh isotopes near $A \sim 104$

C. Vaman PRL92 (2004) 032501, P. Joshi et al., PLB in print.

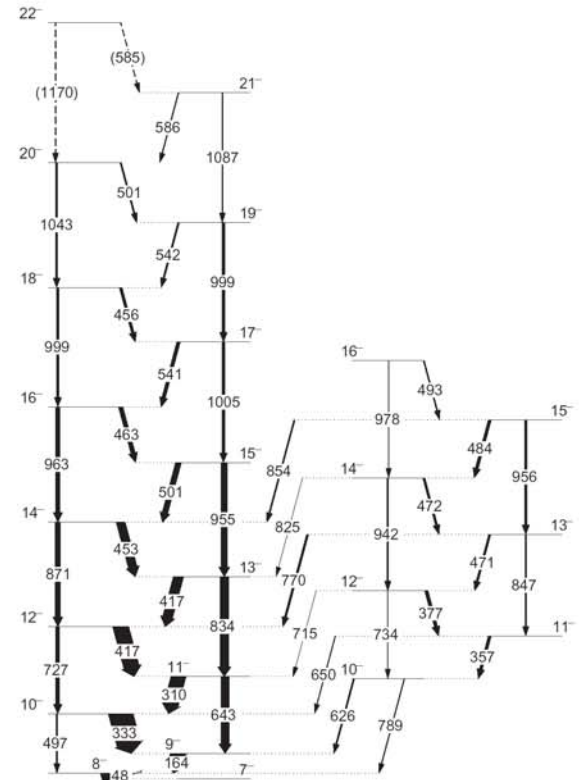
See posters of P.Joshi and C. Vaman



^{102}Rh



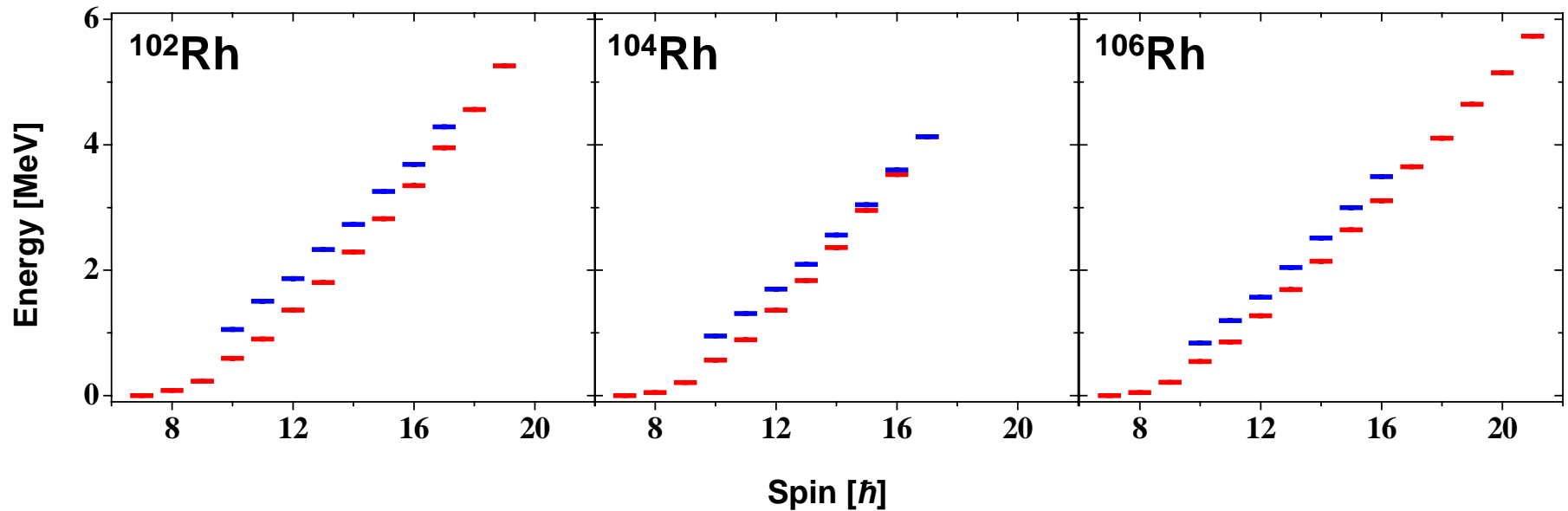
^{104}Rh



^{106}Rh

Systematics of odd-odd Rh isotopes near $A \sim 104$

C. Vaman PRL92 (2004) 032501, P. Joshi et al., PLB in print.

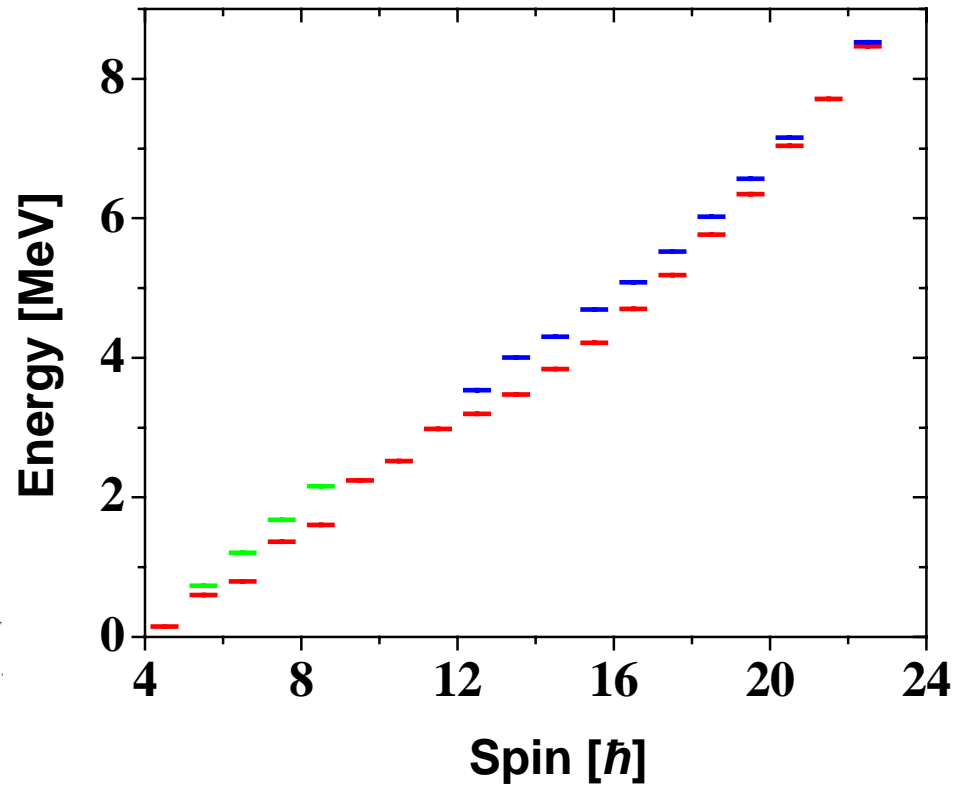
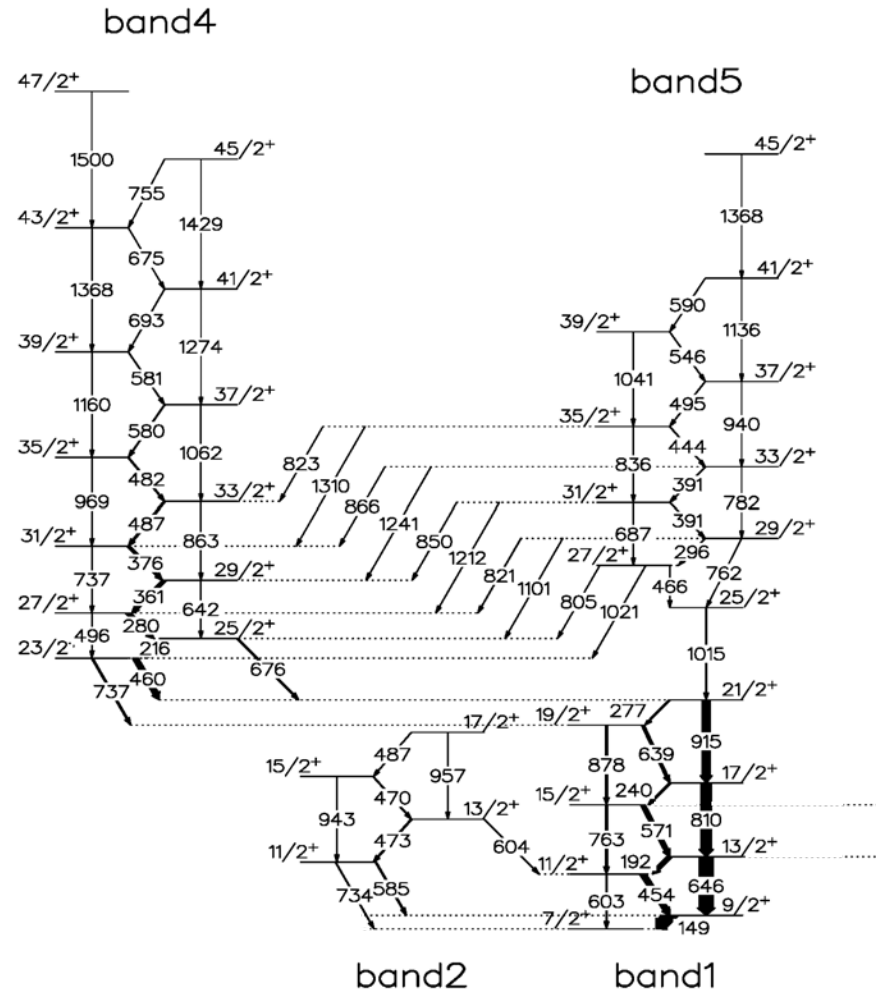


See posters of P. Joshi and C. Vaman

Doublet bands in ^{105}Rh

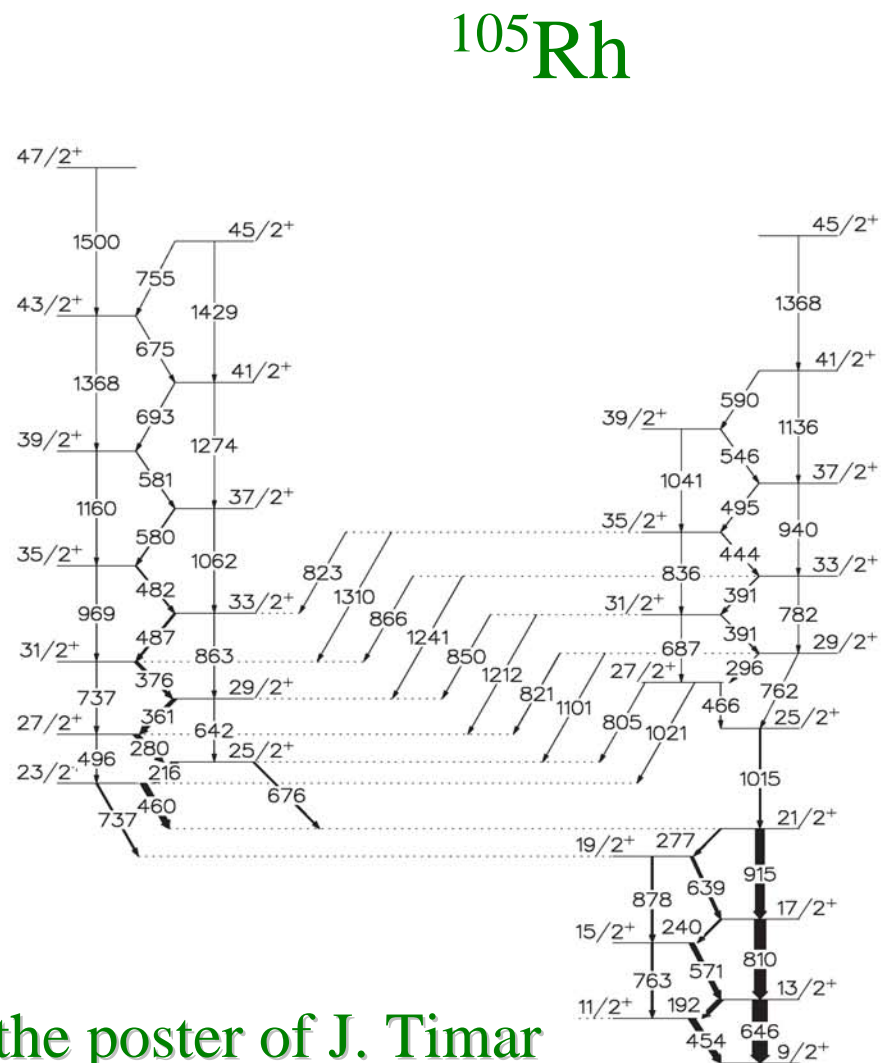
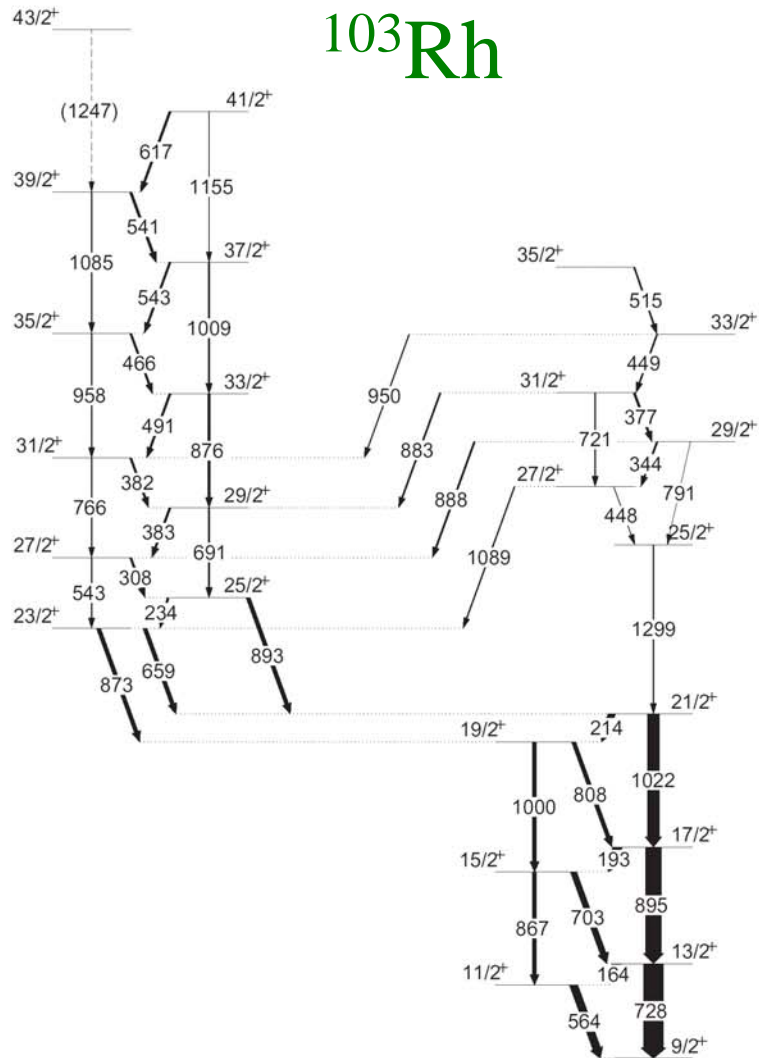
J. Timar et al., submitted to PLB.

See the poster of J. Timar



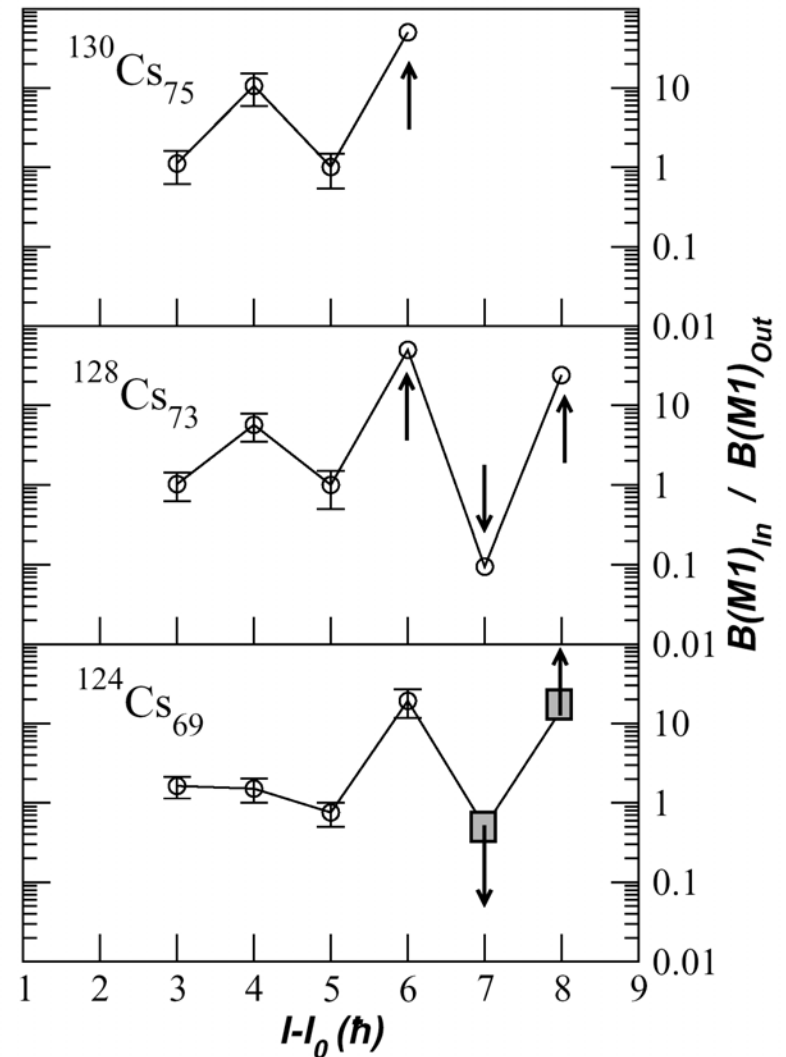
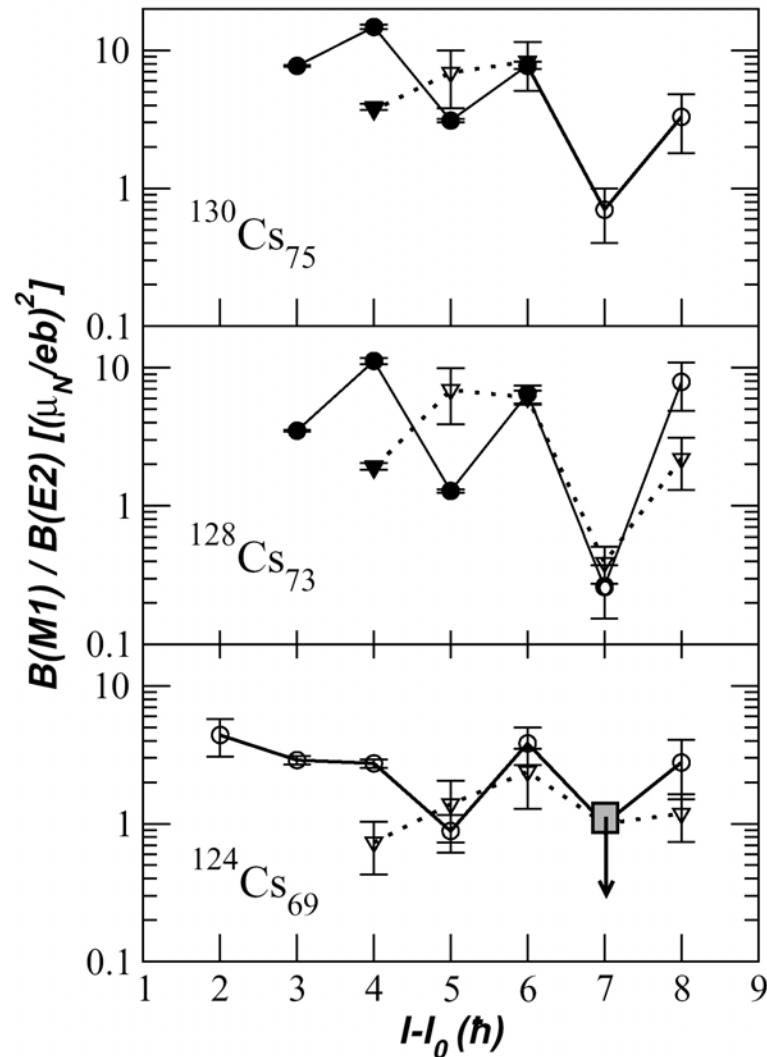
Doublet bands in odd-even ^{103}Rh and ^{105}Rh near ^{104}Rh

C. Vaman et al., J. Timar et al., submitted to PLB.

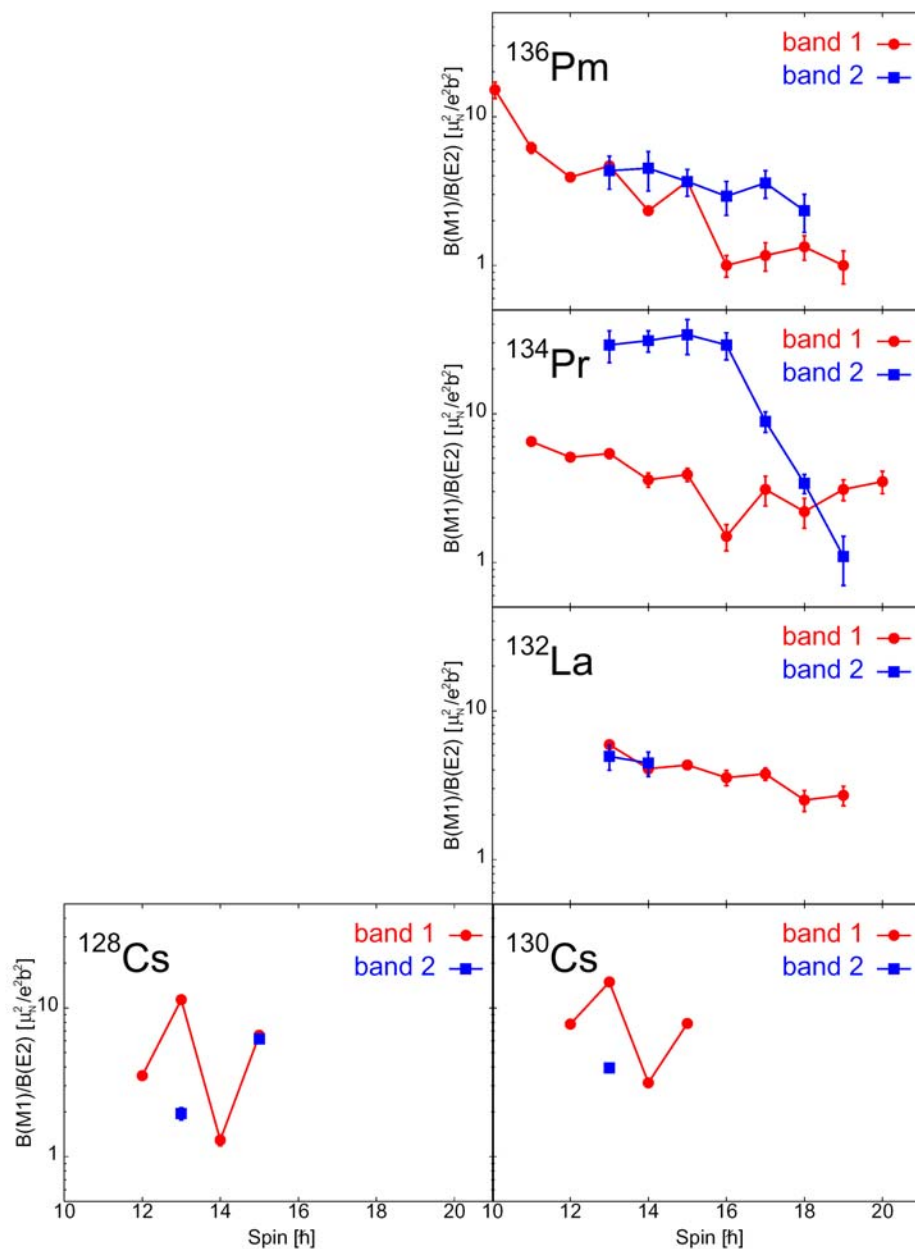


See the poster of J. Timar

Electromagnetic properties – pronounced staggering in experimental $B(M1)/B(E2)$ and $B(M1)_{in} / B(M1)_{out}$ ratios as a function of spin [T.Koike et al. PRC 67 (2003) 044319].



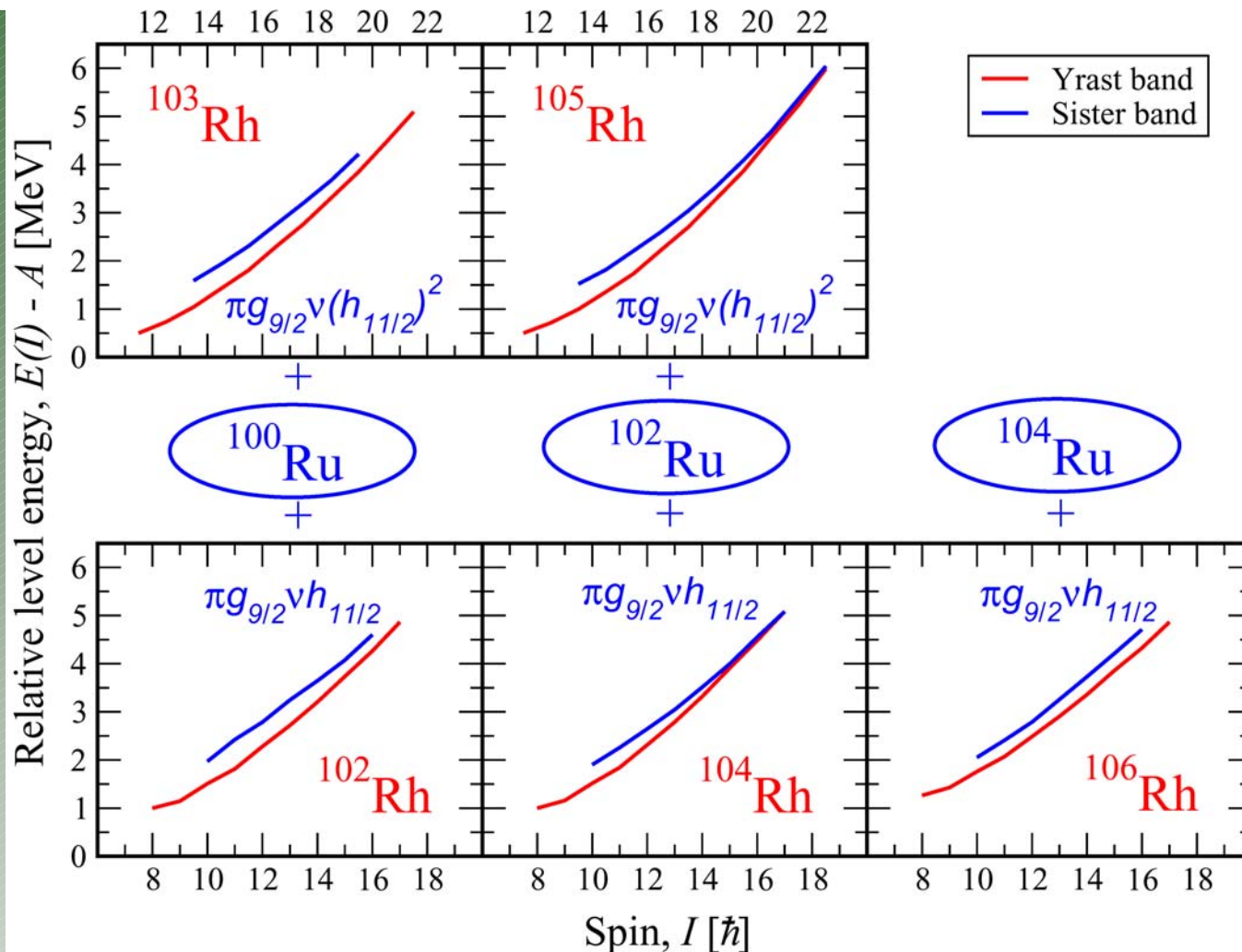
Electromagnetic properties – unexpected $B(M1)/B(E2)$ behavior for ^{134}Pr and heavier $N=75$ isotones.



What have we learned from chirality so far?

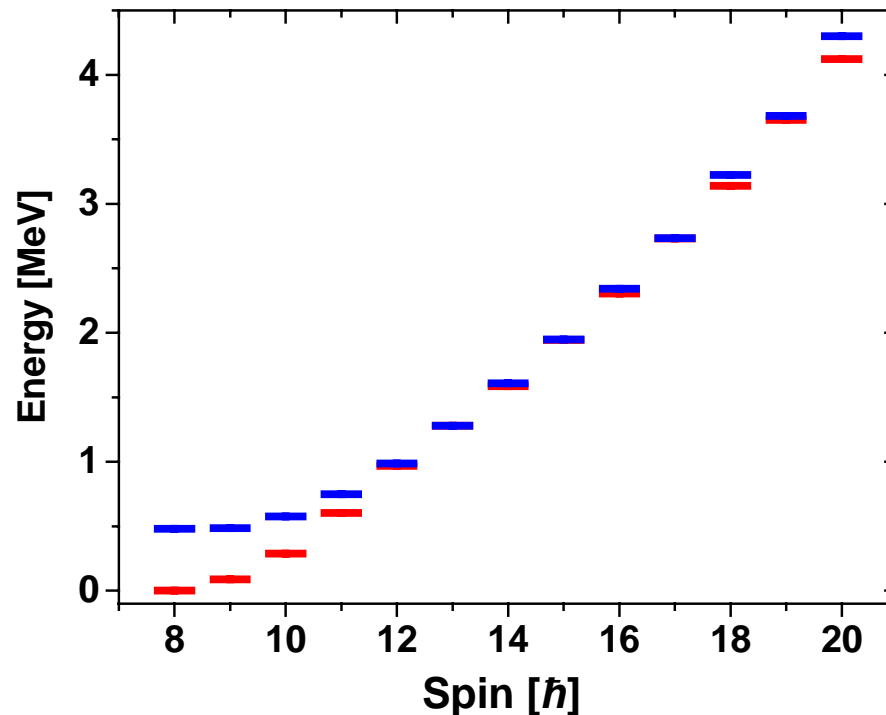
Chirality is a general phenomenon in triaxial nuclei:

- *two mass regions identified up to date,*
- *partner bands in odd-odd and odd-A nuclei.*



Energy separation vs. spin trend understood:

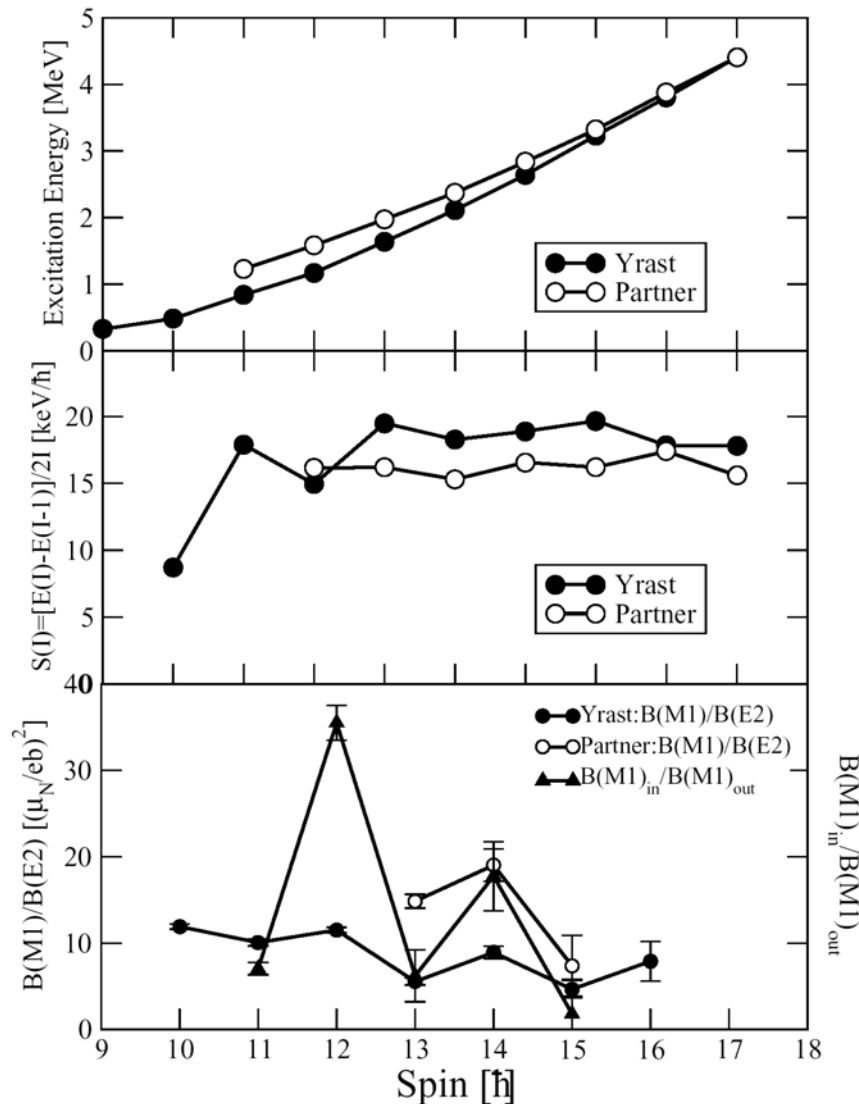
- *planar components at the low spin,*
- *degenerate levels at the medium spin,*
- *Coriolis alignment at the high spin.*



*The smoking gun has been identified:
three fingerprints currently established for
chirality in odd-odd triaxial nuclei:*

- near degenerate doublet $\Delta I=1$ bands for a range of spin I ;*
- $S(I)=[E(I)-E(I-1)]/2I$ independent of spin I ;*
- chiral symmetry restoration selection rules for $M1$ and $E2$ transitions vs. spin resulting in staggering of the absolute and relative transition strengths.*

Based on the above fingerprints ^{104}Rh provides the best example of chiral bands observed up to date.



✓ *doubling of states*

✓ *$S(I)$ independent of I*

✓ *$B(M1)$, $B(E2)$ staggering*

C. Vaman et al. PRL 92(2004)032501

A new limit of particle rotor model for triaxial nuclei has been identified:

For irrotational flow moment of inertia there are two special cases for which two out of three moments are equal:

axial symmetry

for $\gamma=0^\circ$ (prolate shapes)

$$J_s = J_i = J_0 \quad J_l = 0$$

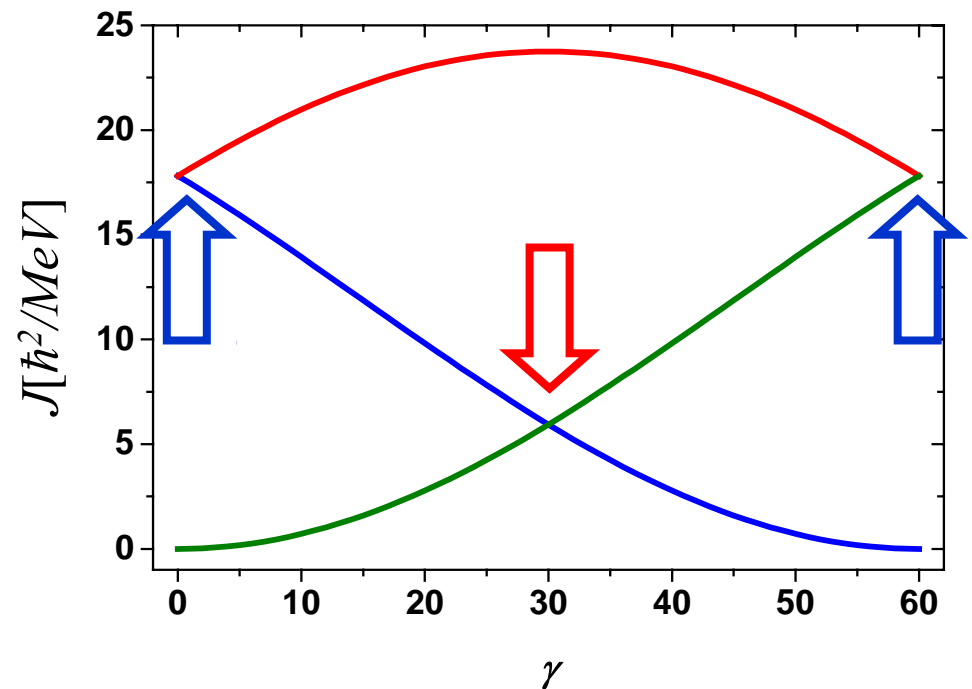
for $\gamma=60^\circ$ (oblate shapes)

$$J_l = J_i = J_0 \quad J_s = 0$$

triaxiality

for $\gamma=30^\circ$ (triaxial shapes)

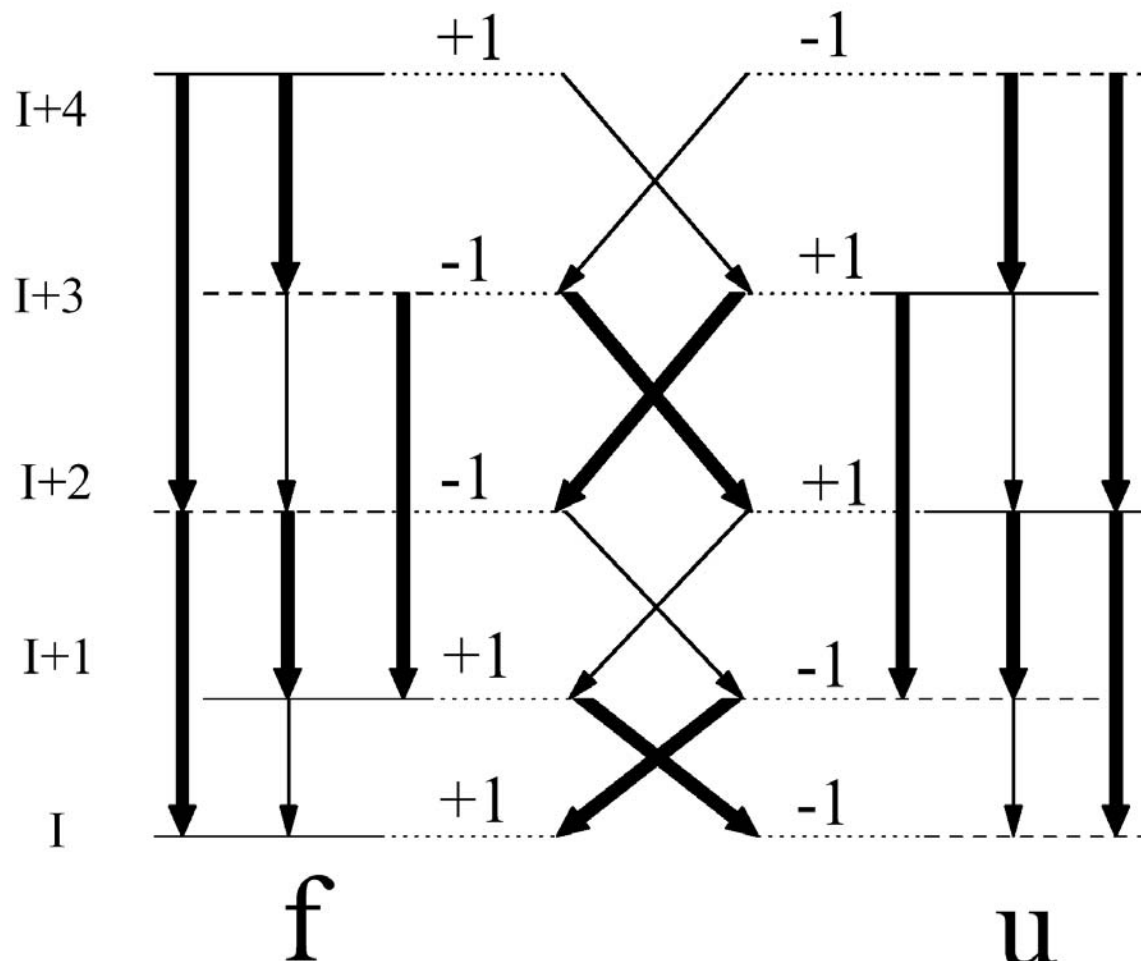
$$J_l = J_s = J_0 \quad J_i = 4J_0.$$



For triaxial shapes at $\gamma=30^\circ$ the rotor hamiltonian has a very similar structure to the hamiltonian for axially symmetric shapes.

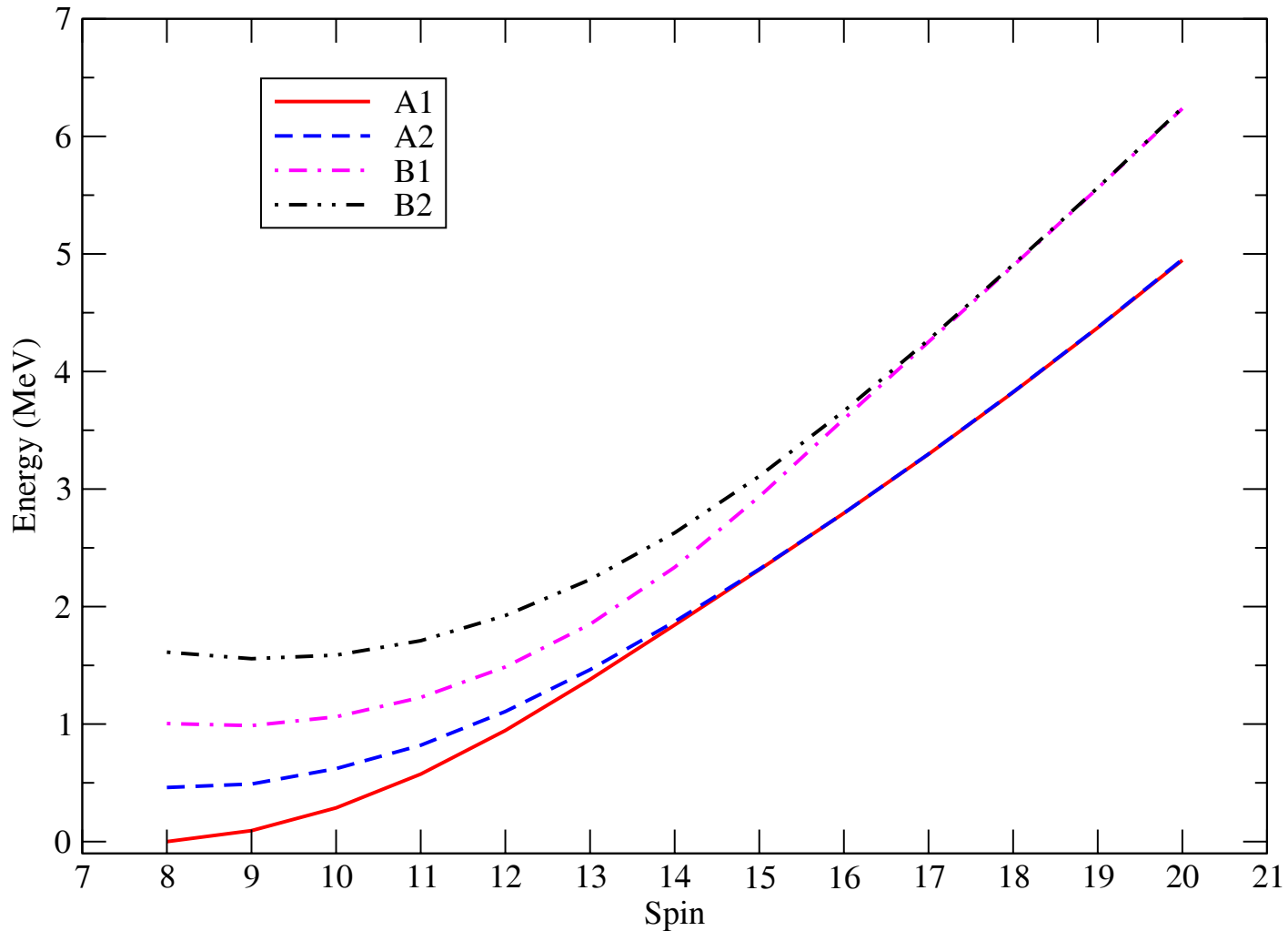
The intermediate axis becomes an effective symmetry axis.

*New symmetry of particle rotor model for odd-odd chiral nuclei:
results in selection rules and unique predictions for
electromagnetic transition rates without a need for calculation.*



T. Koike et al. , submitted to PRL

Conditions for chirality coincide with conditions for wobblers in the model Hamiltonian discussed in the next talk.



Chirality, open questions:

- *electromagnetic properties, transition rates,*
- *when the tunneling between the two handedness is appreciable and in which conditions the tunneling is expected,*
- *the criterion for the chiral bands: the degeneracy of doublet states as compared to rotational frequency.*